

Calculator NOT Permitted**Multiple Choice**

1.	A
2.	A
3.	A
4.	D
5.	E
6.	C
7.	B
8.	C
9.	C

Multiple Choice		
Free Response		
Total out of 18 points		

This reviews the second half of unit 1. Please also study quiz #1 review, each FRQ from the homework, and read over your notes.

FREE RESPONSE

Consider the two piece-wise defined functions, $f(x)$ and $g(x)$, below to answer the questions that follow.

$$f(x) = \begin{cases} \frac{1}{2}x^2 - x + 2, & -4 < x \leq -2 \\ \sqrt{x+6} + 4, & x > -2 \end{cases} \quad g(x) = \begin{cases} \frac{1}{2}x + 4, & x < -4 \\ -\frac{1}{2}x, & x > -4 \end{cases}$$

a. Using interval notation, identify the domain of both functions.

Domain of $f(x)$: $(-4, \infty)$ Domain of $g(x)$: $(-\infty, -4) \cup (-4, \infty)$

+1/2

+1/2

b. Find the values of $f(-2)$ and $g(f(3))$. Show the analysis that leads to your answers.

$$\begin{array}{l|l|l} f(-2) = \frac{1}{2}(-2)^2 - (-2) + 2 & f(3) = \sqrt{(3)+6} + 4 & g(f(3)) = g(7) \\ = \frac{1}{2}(4) + 2 + 2 & = \sqrt{9} + 4 & = -\frac{1}{2}(7) \\ = 2 + 2 + 2 & = 3 + 4 & g(f(3)) = -\frac{7}{2} \\ f(-2) = 6 & f(3) = 7 & \end{array}$$

+1

+1

+1

c. Does $f(x)$ have a discontinuity at $x = -2$? If so, classify the discontinuity, justifying your conclusion.

$$\text{I. } f(-2) = 6 \quad +1$$

$$\therefore f(-2) \text{ is defined.}$$

$$\text{II. } \lim_{x \rightarrow -2^-} f(x) = \frac{1}{2}(-2)^2 - (-2) + 2 = \frac{1}{2}(4) + 2 + 2 = 2 + 2 + 2 = 6$$

$$\lim_{x \rightarrow -2^+} f(x) = \sqrt{(-2)+6} + 4 = \sqrt{4} + 4 = 2 + 4 = 6$$

$$\therefore \lim_{x \rightarrow -2} f(x) \text{ exists} \quad +1$$

$$\text{III } \lim f(x) = f(-2) = 6 \quad +1$$

$$\therefore f(x) \text{ is continuous at } x = -2 \quad +1$$

d. Does $g(x)$ have a discontinuity at $x = -4$? If so, classify the discontinuity, justifying your conclusion.

$$\text{I. } g(-4) \text{ is undefined} \quad +1$$

$$\text{II. } \lim_{x \rightarrow -4^-} g(x) = \frac{1}{2}(-4) + 4 = -2 + 4 = 2$$

$$\lim_{x \rightarrow -4^+} g(x) = -\frac{1}{2}(-4) = 2$$

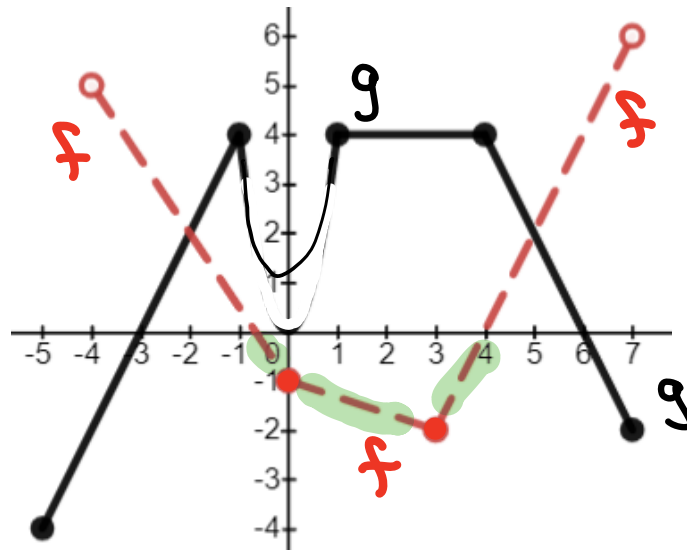
$$\lim_{x \rightarrow -4} g(x) \text{ exists} \quad +1$$

$$\text{III } g(-4) \neq \lim_{x \rightarrow -4} g(x) \quad +1$$

$$\therefore g(x) \text{ has point discontinuity at } x = -4 \quad +1$$

MULTIPLE CHOICE

Use the graph to answer questions 1 and 2. The dashed graph is $f(x)$ and the solid graph is $g(x)$.



1. At which of the following values of x is $f(x) < 0$ and $f(x) < g(x)$?

I. $x = -1$
 $f < 0$ ✓
 $f < g$ ✓
 A. II only

II. $x = 2$
 $f < 0$ ✓
 $f < g$ ✓

III. $x = 4$
 $f < 0$ ✗
 $f < g$ ✓

- B. I and II only
- C. III only
- D. II and III only
- E. I, II, and III

$f(x)$ is below x -axis
 $f(x)$ is below $g(x)$

2. Which of the following best describes where the graph of $g(x) \leq 0$?

A. $[-5, -3] \cup [6, 7]$

B. $(-3, 0) \cup (0, 6)$

C. $(-5, -3] \cup [6, 7)$

D. $[-5, -3] \cup [6, 7]$ and $x = 0$

E. $[-3, 6]$

3. Consider the functions $f(x) = 2x^2 + 3x - 2$ and $g(x) = x - 2$. Find an equation for $(f \cdot g)(x)$.

- A. $(f \cdot g)(x) = 2x^3 - x^2 - 8x + 4$
- B. $(f \cdot g)(x) = 2x^3 - 4x^2 - 5x + 4$
- C. $(f \cdot g)(x) = 2x^2 - 5x$
- D. $(f \cdot g)(x) = x^2 - 8x + 4$
- E. None of these

$$\begin{aligned}
 & (2x^2 + 3x - 2)(x - 2) \\
 &= 2x^3 + 3x^2 - 2x - 4x^2 - 6x + 4 \\
 & \underline{\hspace{1.5cm}} \\
 & 2x^3 - x^2 - 8x + 4
 \end{aligned}$$

4. Identify the domain of the function $g(x) = \frac{3-x}{x^2-x-20}$

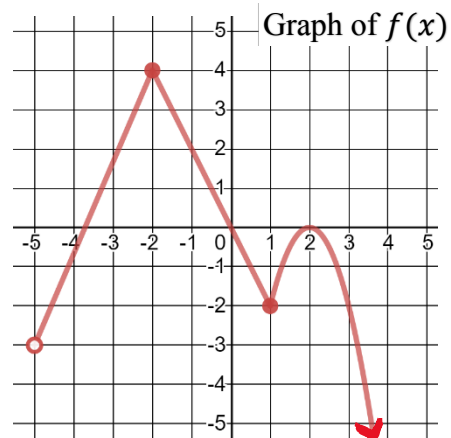
- A. $(-\infty, -4) \cup (-4, 3) \cup (3, 5) \cup (5, \infty)$
- B. $(-\infty, 3) \cup (3, \infty)$
- C. $(-\infty, \infty)$
- D. $(-\infty, -4) \cup (-4, 5) \cup (5, \infty)$
- E. The domain cannot be determined.

Denom $\neq 0$
 $(x-5)(x+4) \neq 0$
 $x-5 \neq 0 \Rightarrow x \neq 5$
 $x+4 \neq 0 \Rightarrow x \neq -4$

5. The graph of $f(x)$ is shown to the right and $g(x) = 5 - 2x$. What is the value of $f(g(5))$?

- A. -3
- B. 7
- C. 19
- D. -2
- E. Undefined

$g(5) = 5 - 2(5) = -5$
 $f(-5)$ is undefined



6. What is the domain of the function $f(x) = \sqrt{9-3x}$.

- A. $[3, \infty)$
- B. $(-\infty, 3)$
- C. $(-\infty, 3]$
- D. $(-\infty, 3) \cup (3, \infty)$
- E. $(3, \infty)$

RADICAND ≥ 0
 $9 - 3x \geq 0$
 $-3x \geq -9$
 $x \leq 3$

7. For what value of a would the function $g(x) = \begin{cases} ax - 3, & x < -2 \\ x^2 - 2x, & x > -2 \end{cases}$ have a point discontinuity at $x = -2$.

A. $a = \frac{5}{2}$

B. $a = -\frac{11}{2}$

C. $a = -\frac{5}{2}$

D. $a = -\frac{3}{2}$

E. No value of a will make the function have a point discontinuity at $x = -2$.

$$\lim_{x \rightarrow -2^-} (ax - 3) = \lim_{x \rightarrow -2^+} (x^2 - 2x)$$

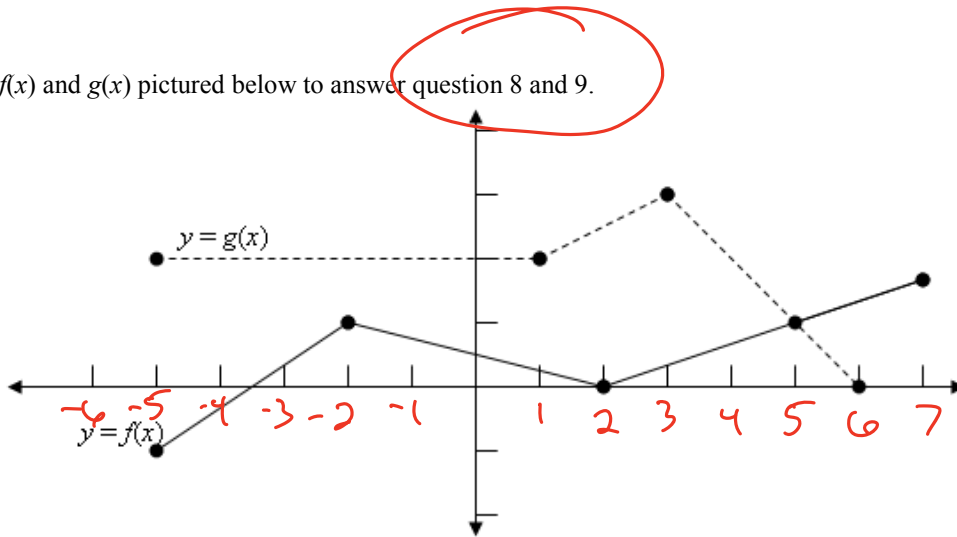
$$a(-2) - 3 = (-2)^2 - 2(-2)$$

$$-2a - 3 = 4 + 4$$

$$-2a = 11$$

$$a = -\frac{11}{2}$$

Use the graphs of $f(x)$ and $g(x)$ pictured below to answer question 8 and 9.



8. Which of the following statements is/are true about the graphs of $f(x)$ and $g(x)$?

I. $f(x)$ is increasing on the intervals $(-5, -2)$ and $(2, 7)$. ✓

II. $f(x) = g(x)$ only at $x = 5$. ✓

III. $f(x) > g(x)$ only on the interval $(5, 6)$. ✓

A. I only

B. I and II only

C. I, II and III

D. II and III only

E. II only

9. If $p(x) = 2mx^2 - 3x$, for what value(s) of m would $p(-1) = f(g(0))$?

A. $m = -\frac{1}{2}$

B. $m = \frac{5}{2}$

C. $m = -\frac{3}{2}$

D. $m = \frac{3}{2}$

E. No value of m would make $p(-1) = g(f(0))$.

$$2m(-1)^2 - 3(-1) = f(g(0))$$

$$2m(1) + 3 = f(2)$$

$$2m + 3 = 0$$

$$2m = -3$$

$$m = -3/2$$